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Tractionless Self-Propulsion of Active Drops

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We report on a new mode of self-propulsion exhibited by compact drops of active liquids on a substrate which, remarkably, is tractionless, i.e., which imparts no mechanical stress locally on the surface. We show, both analytically and by numerical simulation, that the equations of motion for an active nematic drop possess a simple self-propelling solution, with no traction on the solid surface and in which the direction of motion is controlled by the winding of the nematic director field across the drop height. The physics underlying this mode of motion has the same origins as that giving rise to the zero viscosity observed in bacterial suspensions. This topologically protected tractionless self-propulsion provides a robust physical mechanism for efficient cell migration in crowded environments like tissues.

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Self-propulsion, in the absence of load, is required by Newton's laws to be force-free. This is ubiquitous in the locomotion of microorganisms where inertia is negligible, from swimming bacteria to crawling cells. By force-free, one means that the *total* force exerted by the environment on the motile entity is zero (and the other way around). This is usually achieved by a gradient of nonzero *local forces* on the boundary, as exemplified by cells crawling on a surface which push at the front and pull at the back. It would appear impossible to achieve *traction-free* self-propulsion, that is, with local forces which not only sum up to zero but are identically zero everywhere [1]. However, in this Letter, we demonstrate that such self-propulsion is indeed possible for active matter, such as the cytoskeleton of living cells. This mode of motion is not possible in objects driven at boundaries but can occur only for those driven in the bulk.

Eukaryotic cells have the ability to move in a variety of complex environments, and they do so by adapting their mode of migration to the geometrical and physical properties of their surroundings [2,3]. Crawling is a mode of motility well characterized experimentally [4–6] and captured by a variety of physical models [7–12]. In crawling, forces are transmitted through local friction, which is provided by the focal adhesions that connect the cytoskeleton to a surface or to the extracellular matrix. However, these adhesions are structurally unstable at high strain rates [13]. This makes crawling ineffective for fast migration in tissues, where cells have to squeeze through tiny gaps. Motion with zero local force does not have this limitation, with profound implications.

A minimal model to study the physical principles of motility consists of a drop of viscous liquid with orientable components that consume energy (active matter) on a flat rigid surface and confined by surface tension. A drop of active matter generates internal flows all by itself due to

energy input from its components [14–18], and these can cause the drop to move spontaneously [11,19–27]. Several studies have shown propulsion of active drops on a surface with a number of related models [7,9–12]. But those invariably involve local forces (in the form of friction) on the substrate.

In this Letter, we show that an active drop can propel itself without exerting any traction—defined as the local tangential force per unit area—anywhere on the substrate, except at its very edge due to surface tension acting to maintain the drop shape (Fig. 1). This tractionless self-propulsion is controlled by the global topology of the orientable active units and also allows motion in a confined geometry. Specifically, we consider a thin drop endowed with active stresses $\sigma_{ij}^a = -\alpha n_i n_j$ ($\alpha \neq 0$ is the signature of activity) induced by active units whose orientations are characterized by a local director \mathbf{n} (a unit vector), and we demonstrate that the equations of motion of this drop on a surface possess a tank-treading solution, which results in a center-of-mass velocity given *exactly* by

$$V = \frac{\alpha H}{2\pi\omega\eta}, \quad (1)$$

where H is a characteristic drop height (whose definition will be made more precise), η is the fluid viscosity, and ω is the (nonzero) winding number defined as the number of quarter turns of the director across the drop height. The signature of this novel mode of propulsion is the zero tangential traction exerted by the drop on the substrate except at the drop edges due to finite contact angles.

Our model is a 2D drop of active nematic liquid crystal [14,15,17,18] moving with (unknown) velocity V on a solid substrate. The drop shape is described by its thickness $h(x, t)$ in the normal direction (z) as a function of its in-plane position (x), as illustrated in Fig. 2(a). We seek

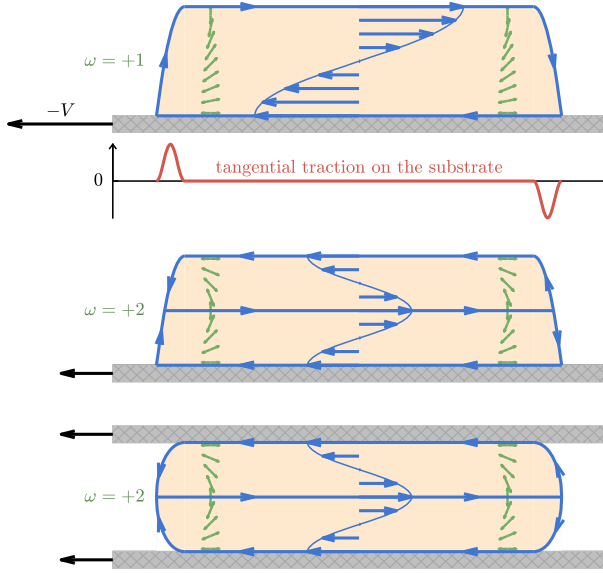


FIG. 1. Tractionless self-propulsion of an active drop. A drop with active stresses $\sigma_{ij}^a = -an_i n_j$ propels itself (here rightward) at velocity V , given by Eq. (1), without exerting any tangential traction on the substrate (except locally at its edges: this local traction is solely due to surface tension acting to maintain the drop shape). The winding number ω , defined as the number of quarter turns of the director \mathbf{n} (green rods) across the drop height, controls the number of fluid circulation cells inside the drop. The internal velocity profile (blue arrows) in the comoving frame of reference is $u_x = -V \cos(\omega\pi z/H)$, with z being the distance to the substrate, and yields a tank-treading type of motion. The solution obtained for $|\omega| = 2$ also allows propulsion in a confined geometry.

traveling wave solutions $h = h(x - Vt)$ which must satisfy, from mass conservation,

$$\int_0^h u_x dz = Vh, \quad (2)$$

where \mathbf{u} is the fluid velocity inside the drop, which is assumed to be incompressible ($\partial_i u_i = 0$).

The velocity in Eq. (2) can be obtained by solving the Stokes flow equation [28]

$$\partial_j \sigma_{ij} = 0, \quad (3a)$$

with

$$\sigma_{ij} = -p\delta_{ij} + \eta(\partial_j u_i + \partial_i u_j) - an_i n_j, \quad (3b)$$

where p is the pressure and where the director $\mathbf{n} = (\cos\theta, \sin\theta)$ minimizes the nematic free energy in the *strong* elastic limit [30]: $\nabla^2\theta = 0$ with boundary conditions $\theta = 0$ at $z = 0$ (anchoring parallel to the substrate) and $\theta = \omega\pi/2 + \arctan(h')$ at $z = h$ (fixed angle $\omega\pi/2$ with respect to the free surface tangent) [31]. In this limit, while

the director will affect the flow, the back coupling of the flow on the director is negligible.

At the liquid-solid interface, the interaction of the drop with the rigid substrate is modeled by a partial slip boundary condition:

$$u_x = \ell_u \sigma_{xz}/\eta \quad \text{at } z = 0, \quad (4a)$$

where ℓ_u is a slip length. At the gas-liquid interface, we use a free surface boundary condition:

$$\boldsymbol{\sigma} \cdot \mathbf{m} = \gamma \kappa \mathbf{m} \quad \text{at } z = h, \quad (4b)$$

where \mathbf{m} is the unit outward vector normal to the free surface, γ is the surface tension, and $\kappa = -\nabla \cdot \mathbf{m}$ is the signed curvature.

Assuming a thin droplet geometry where variations in the x direction are much slower than in the z direction ($\partial_x \ll \partial_z$), as is now standard [12,34–36], we can derive a leading-order explicit expression of u_x as follows. It can be shown that if $\omega = 0$, the drop is static. Therefore we choose $\omega \neq 0$, and the director orientation reads, at leading order,

$$\theta = \frac{\omega\pi z}{2h}, \quad (5)$$

and $\omega \in \mathbb{Z}^*$ is effectively a winding number which counts the number of quarter turns of the director across the drop height, as illustrated in Fig. 2(a).

The z component of Eq. (3) gives, at leading order, $\partial_z p = 0$, and using the normal component of Eq. (4b), we find that $p = -\gamma h''$. The x component of Eq. (3) yields $\partial_z \sigma_{xz} = \partial_x p$. This can be integrated once in z , and we find, using the tangential component of Eq. (4b) and substituting p , that

$$\sigma_{xz} = -\gamma h'''(z - h). \quad (6)$$

Substituting the definition of σ_{xz} into Eq. (6) and integrating once in z with Eq. (4a) yields the parallel velocity

$$u_x = -\frac{\gamma}{\eta} \left(\frac{z^2}{2} - (z + \ell_u)h \right) h''' + \frac{\alpha(1 - \cos 2\theta)}{\eta 2\pi\omega} h. \quad (7)$$

As a last step, we integrate Eq. (7) over the drop thickness to obtain, using Eq. (2), a nonlinear third-order ordinary differential equation for the steady-state shape of the drop

$$\frac{\gamma}{\eta} \left(\frac{h^2}{3} + \ell_u h \right) h''' + \frac{\alpha}{\eta 2\pi\omega} h = V \quad (8)$$

on the domain $x \in [-L/2, L/2]$ with four boundary conditions at the contact lines:

$$h(\pm L/2) = 0, \quad h'(\pm L/2) = \mp\phi, \quad (9)$$

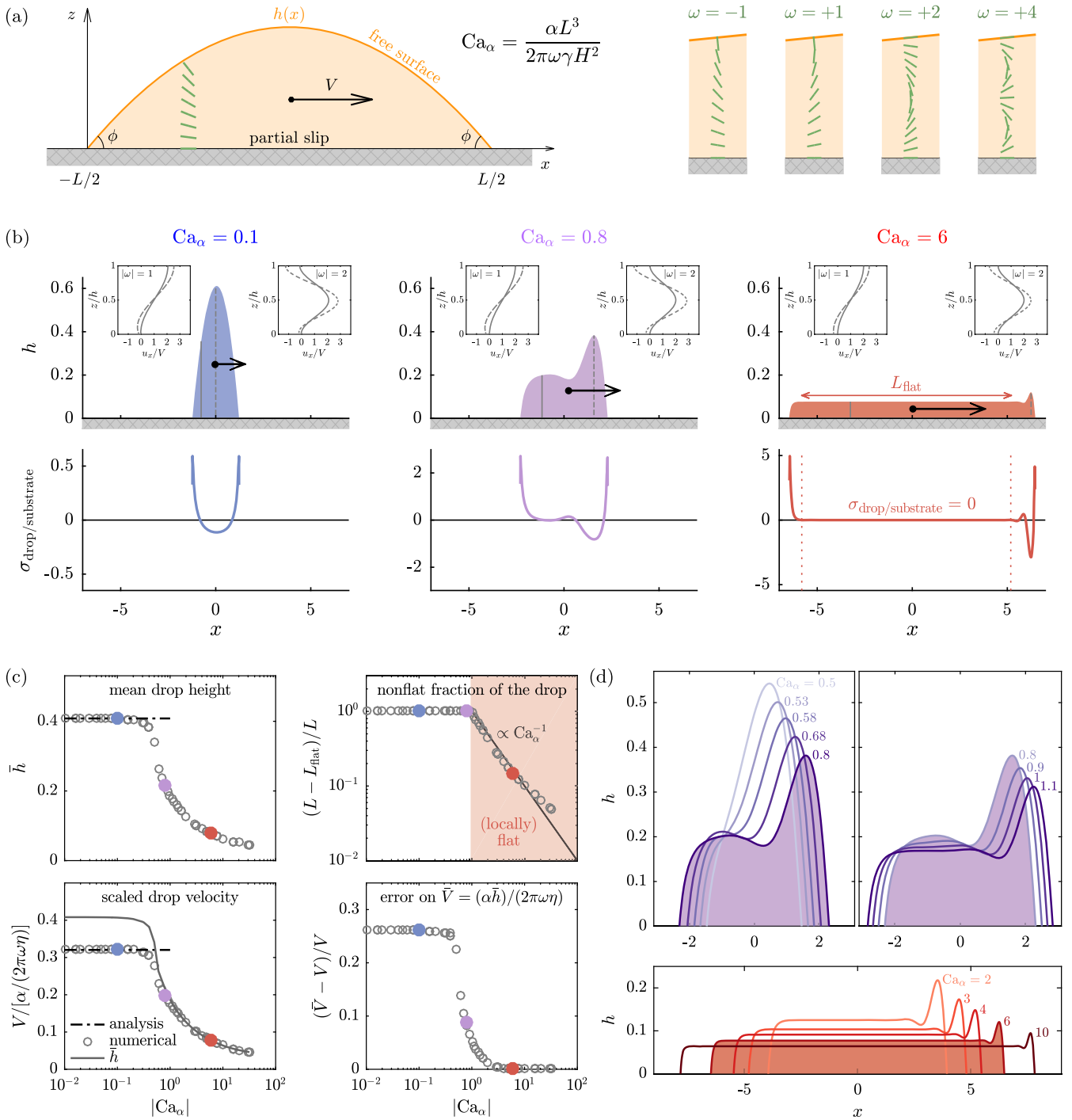


FIG. 2. (a) Model of a thin active drop with a wound director bounded by a partial slip surface and a free surface. The drop shape and velocity are controlled by $Ca_\alpha = (\alpha L^3)/(2\pi\omega\gamma H^2)$, where ω is the winding number. (b) Drop shape and tangential traction exerted on the substrate in the three regimes of Ca_α . (Insets) Internal velocity profiles in selected cross sections for $|\omega| = 1$ and $|\omega| = 2$. (c) Effect of Ca_α on the drop geometry and velocity: \bar{h} is the mean height of the drop, $(L - L_{\text{flat}})/L$ is the fraction of the drop which is not flat, and \bar{V} is the estimate of the drop velocity based on the exact solution given by Eq. (1) and using the mean height \bar{h} as an approximation for H . (d) Dependence of the drop shape on Ca_α (top panels) in the transitional regime and (bottom panel) at high Ca_α .

where ϕ is the prescribed contact angle. The drop velocity V is an unknown constant determined as part of the solution, and the drop width L is determined by the volume constraint (set here to unity)

$$\int_{-L/2}^{L/2} h dx = 1. \quad (10)$$

Dimensional analysis of Eq. (8) indicates that the drop shape is controlled by $\text{Ca}_\alpha = (\alpha L^3)/(2\pi\omega\gamma H^2)$, which can be understood as the active equivalent of the capillary number $\text{Ca}_\alpha = (\eta V L^3)/(\gamma H^3)$ with V given by Eq. (1). Since $\text{Ca}_\alpha(\alpha, \omega) = \text{Ca}_\alpha(-\alpha, -\omega)$, changing the direction in which the director winds (from counterclockwise to clockwise) is equivalent to changing the sign of activity (from extensile to contractile). Furthermore, if $\{h(x), V\}$ is a solution for Ca_α , then $\{h(-x), -V\}$ is a solution for $-\text{Ca}_\alpha$: reversing the sign of Ca_α simply reverses the direction of motion.

Stable solutions of Eqs. (8)–(10) were obtained by solving numerically the time-dependent problem until it reaches steady state for various Ca_α (see the Supplemental Material [29] for details about numerical methods, in all simulations $\ell_u = 0.05$ and $\phi = 1$). This allowed us to identify two regimes of low and high Ca_α separated by a transition region around $\text{Ca}_\alpha \approx 0.8$, as shown in Figs. 2(b) and 2(c).

For low Ca_α , the drop shape is close to a parabola (the equilibrium solution for a passive drop), and a perturbation analysis gives the solution [shown with dashed-dotted lines in Fig. 2(c)]

$$V = \frac{\alpha}{2\pi\omega\eta} \frac{\phi L \sqrt{b} - (b-1) \text{arctanh}(1/\sqrt{b})}{4 \text{arctanh}(1/\sqrt{b})}, \quad (11)$$

where $b = 1 + 12\ell_u/(L\phi)$ and $L = \sqrt{6/\phi}$.

At intermediate Ca_α , the drop undergoes a continuous transition to a qualitatively different shape over a narrow range of Ca_α , here for $0.58 < \text{Ca}_\alpha < 1$ (the numerical values of the boundaries of the transition regime depend on ℓ_u and ϕ). First, at $\text{Ca}_\alpha = 0.58$, the drop develops a frontal bump [$h(x)$ goes from having one extremum to three extrema; see Fig. 2(d), top left panel]. Then, at $\text{Ca}_\alpha = 1$, the drop starts flattening at the rear [Fig. 2(d), top right panel].

For high Ca_α , the drop spreads and the extent of the flat region grows rapidly with increasing Ca_α [Fig. 2(c), top right panel]. Analysis of the numerical data indicates that after the transition, the nonflat fraction of the drop initially decreases as Ca_α^{-1} . The drop velocity can be shown from the governing equation to be given exactly by Eq. (1), where H is the local height of the drop where $h''' = 0$. In practice, V can be estimated by using the mean drop height as an approximation for H [Fig. 2(c), bottom right panel]. The error is 5% at $\text{Ca}_\alpha = 1$ and goes to zero as $\text{Ca}_\alpha \rightarrow \infty$.

The tangential traction exerted by the drop on the substrate is $\sigma_{\text{drop/substrate}} = \sigma_{xz}|_{z=0} = \gamma h h'''$; therefore $\sigma_{\text{drop/substrate}}$, induced by a moving flat drop, is identically zero except at the drop edges [Fig. 2(b), right panel]. It also follows that the drop motion is unaffected by wall slip ℓ_u . Integrating $\sigma_{\text{drop/substrate}}$ over an edge yields an inward force of magnitude $F_{\text{edge/substrate}} = \gamma\phi^2/2$. As seen from the substrate, the drop effectively acts as a contractile force dipole due to finite contact angle ϕ , independent of the sign and magnitude of activity.

This leads us to offer a very simple sketch of the tractionless self-propulsion of a flat drop in Fig. 1. The winding of the director generates an active stress in the liquid which must be balanced by the viscous stress such that the total shear stress vanishes. This creates a number of fluid circulation cells inside the drop exactly equal to $|\omega|$. More precisely, the velocity profile is sinusoidal (compared to parabolic in other modes of motion) and reads, in the laboratory frame of reference,

$$u_x = V \left[1 - \cos\left(\frac{\omega\pi z}{H}\right) \right]. \quad (12)$$

The net flow is not zero and causes the drop to tank tread at a speed V given by Eq. (1). Inside the drop, the rate of viscous dissipation $D^\eta = (\eta\pi^2\omega^2 V^2 L)/(2H)$ is exactly compensated for by the power input $D^a = -(\alpha^2 H L)/(8\eta)$ due to activity. The drop speed is maximal for $|\omega| = 1$. Higher winding numbers, while less favored energetically, are observed in passive nematics with weak anchoring boundary conditions [37] and therefore may still be relevant.

Note that for $|\omega| = 1$, $\sigma_{xz} = 0$, while the macroscopic strain rate $S = H^{-1} \int_0^H \partial_z u_x dz = 2V/H$ is nonzero, meaning that the apparent viscosity of this drop, defined by $\eta_{\text{app}} = \sigma_{xz}/S$, is zero. An analogous mechanism is responsible for the superfluidlike behavior of active suspensions under shear [38–40].

The solution for $|\omega| = 2$ has zero fluid velocity and zero shear stress at *both* boundaries, and therefore it is also a solution for a drop propelling itself in a channel (bottom panel in Fig. 1). Traction maps would show a zero traction on the channel walls everywhere except at the drop edges (the direction and magnitude of these localized forces depend on the wettability of the walls). The latter setup is perhaps the easiest to control experimentally: one can imagine confining a drop of bacterial suspension [38,40] or of microtubule-kinesin mixture [19] between two surfaces, one used for imaging the traction maps [41,42], and the other prepared to ensure appropriate anchoring (through manipulation of the surface chemistry or architecture; see, e.g., Refs. [43–45]).

Unlike other modes of autonomous motion, tractionless tank treading is effective even in the absence of local friction and is not associated with shape anisotropy. These distinctive features are characteristic of contraction-based

amoeboid motility under conditions of weak adhesion and strong confinement, such as those exhibited by leukocyte and human breast cancer cells squeezing through complex 3D extracellular geometries [46,47] or by confined cells migrating in microchannels [2,48]. Because it does not rely on adhesion, this novel mode of self-propulsion provides an efficient mechanism for fast cell motion in crowded environments.

Tractionless self-propulsion is driven by the internal fluid flow in the bulk and is not affected by the details of the edges near the contact line; therefore we expect this mechanism to extend directly to 3D. It is interesting to make a comparison with driving due to a constant shear stress at the free surface (e.g., Marangoni or wind stresses) [49–51] because it gives rise to an identical driving term in the height equation (8). Hence we expect the frontal “bump” seen in 2D to turn into a fingering instability in 3D. However, this similarity is rather superficial, as these boundary-driven advancing fronts have very different internal mechanics from our problem: without the internal stress balance and the activity-driven bulk internal flows, they cannot exhibit tractionless self-propulsion. Finally, the internal flow, caused here by a prescribed winding of the director, could also be induced spontaneously [52]; we leave the analysis of this more mathematically intricate problem for future work.

In conclusion, we have shown that autonomous propulsion, which is always force-free, can also be traction-free. In other words, active materials, by virtue of being bulk driven, can move without imparting any force on their environment. This rather counterintuitive result, derived analytically and confirmed by numerical simulations, is a new example of the astonishing mechanical behavior exhibited by active fluids, like spontaneous flows [19,52–54], zero viscosity [38,40], and nonmonotonic flow curves [39].

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